

## *Chapter 6. Surface Properties of Nanoparticles*

## 6.1 Surface Energy

Surface energy: energy required to create a unit area of new surface

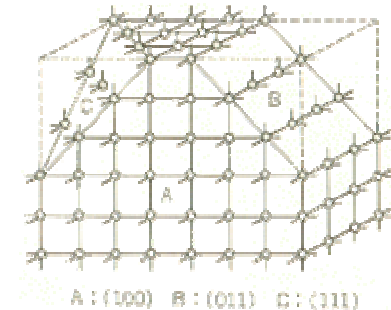
$$\sigma = \left( \frac{\partial G}{\partial A} \right)_{n_i, T, P}$$

Can be represented roughly  $\sigma = \frac{1}{2} N_b \epsilon \rho_a$

where  $N_b$ : number of broken bonds by forming new surface

$\epsilon$  : half of bond strength

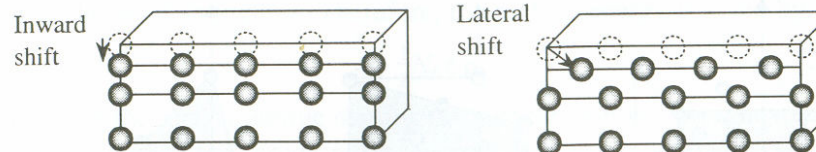
$\rho_a$  : surface atomic density



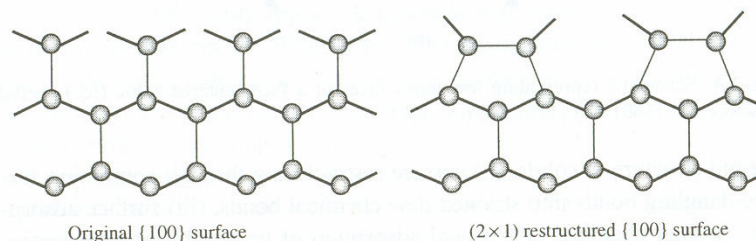
Unsaturated coordination on surfaces

Strong tendency for a solid or a liquid to minimize the total surface energy by

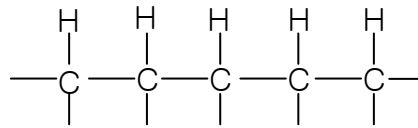
- Surface relaxation: inward shift of surface atoms or ions



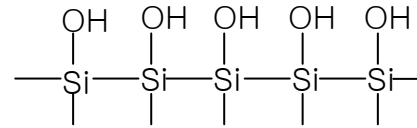
- Surface restructuring



*-Chemical and physical adsorption on its surface*



Diamond surface



Silicon surface

*-Surfactant*

*-composition segregation or enrichment of impurities on surfaces*

*cf. Surface roughening above a transition temperature due to thermal motion*

*-Combination of individual structures together to form large structures*

*- reduce the overall surface energy*

*-Sintering: individual structures merge together*

*-Ostwald ripening: growth of large particles at the expense of smaller particles*

*-Agglomeration : do not alter the individual structures*

*-The smaller agglomerates, the stronger association*

Effect of surface curvature on surface energy

Moving some mass ( $dV \text{ cm}^3$ ,  $dn$  molecules) from flat surface to a particle with a

radius  $R$ ,  $dV = \frac{\pi}{2} d_p^2 dd_p = v_m dn$  and  $dA = \pi d_p dd_p$

Where  $v_m$ : molecular volume (can be  $v_a$  for metals)

Work per atom moved

$$\Delta\mu = \mu_{ps} - \mu_{\infty} = \sigma \frac{dA}{dn} = \sigma \frac{dA}{dV / v_m}$$

$$\therefore \Delta\mu = \sigma \frac{v_m}{d_p} \quad \text{Young-Laplace equation}$$

For any curved surface

$$\Delta\mu = \sigma v_m \left( \frac{1}{R_1} + \frac{1}{R_2} \right)$$

For convex surface,  $R_1, R_2$ : positive: increase in surface potential

For concave surface the reverse is true!

*Form flat surface of liquid to vapor,*

$$\mu_v - \mu_\infty = -kT \ln p_\infty$$

*From curved surface to vapor,*

$$\mu_v - \mu_c = -kT \ln p_c$$

$$\therefore \mu_c - \mu_\infty = \Delta\mu = kT \ln \frac{p_c}{p_\infty}$$

*Combining with (\*)*

$$\ln\left(\frac{p_c}{p_\infty}\right) = \sigma v_m \frac{R_1^{-1} + R_2^{-1}}{kT}$$

*Form spherical particles*

$$\ln\left(\frac{p_c}{p_\infty}\right) = \frac{4\sigma v_m}{d_p kT} \quad \text{Kelvin equation}$$

*Similarly for particles in liquid*

$$\ln\left(\frac{c_c}{c_\infty}\right) = \sigma v_m \frac{R_1^{-1} + R_2^{-1}}{kT}$$

*\*Ostwald ripening*

- Raising temperature to some extent promotes Ostwald-ripening...
- Combined sintering and Ostwald ripening lead to inhomogeneous microstructures...

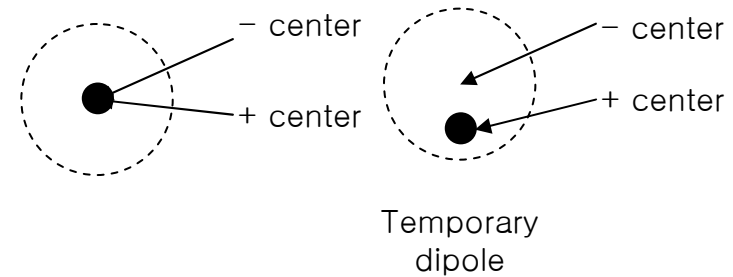
## 6.2 Particle-Particle Interaction

(1) van der Waals force

- Attractive force between temporary dipoles and induced dipoles ("universal" force)

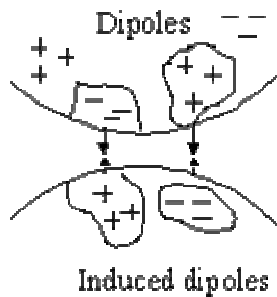
Starting from instantaneous (temporary) dipoles in an atom

"Universal" force



\* Attraction potential:

- Obtained by integrating the forces between all dipole pairs in two bodies



$$\Phi_A = -\frac{A}{6} \left\{ \frac{d_p^2/2}{S^2 + 2d_p S} + \frac{d_p^2/2}{S^2 + 2d_p S + d_p^2} + \ln \left( \frac{S^2 + 2d_p S}{S^2 + 2d_p S + d_p^2} \right) \right\}$$

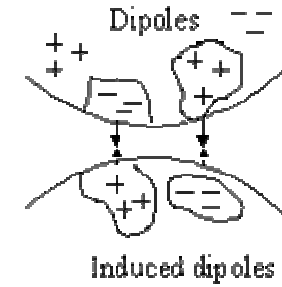
where  $A$ : Hamaker constant ( $\sim 10^{-19} \sim 10^{-20} \text{ J}$ )

when  $S \ll d_p/2$

$$\Phi_A = -\frac{A d_p}{24S}$$

Hamaker constants ( $A$ ) of materials

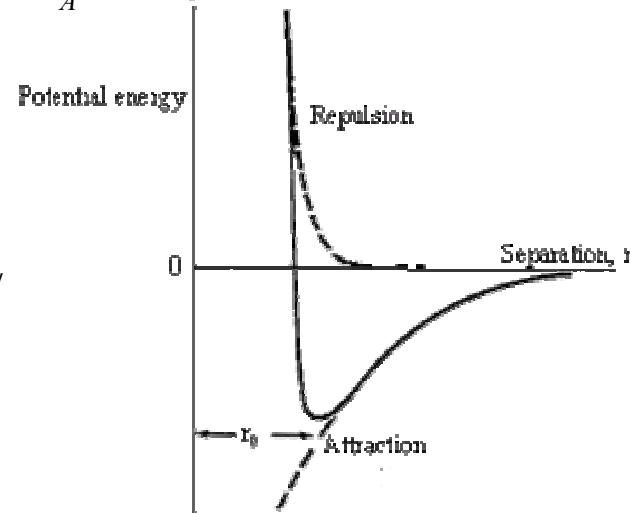
Interacting solids			Hamaker constant, $A(10^{-20} \text{ J})$	
solid	media	solid	Calculated	Measured
Quartz	Vacuum (air)	Quartz	6.5	5-6
Mica	Vacuum (air)	Mica	10	13.5
Metals	Vacuum (air)	Metals	30-50	-
PTFE	Vacuum (air)	PTFE	3.8	-
Quartz	Water	Quartz	8.83	-
Mica	Water	Mica	2.0	2.2
PTFE	Water	PTFE	0.33	-
(Air)	Water	(Air)	3.7	-
Quartz	Water	(Air)	-1.0	-



cf. Molecular attraction potential

$$\Phi_A \propto S^{-6}$$

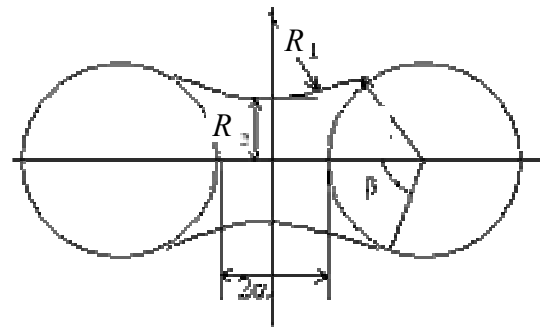
Lennard-Jones(6-12) potential



(2) *Liquid-bridge*

*Formation of water- film bridge between two particles condensed from water vapor*

- *For pendular state*



*Assuming complete wetting*

$$F = 2\pi R_2 \sigma + \pi R_2^2 \sigma \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

*From geometric consideration*

$$F = \frac{\pi d_p \sigma}{1 + \tan(\beta / 2)}$$

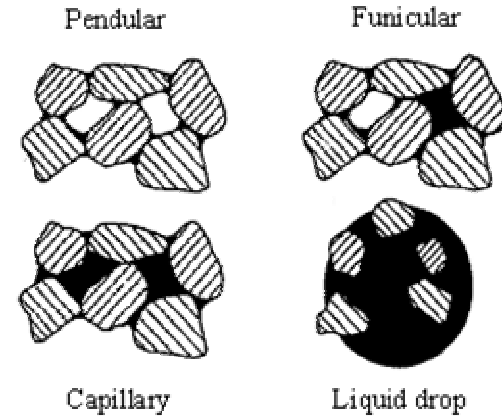
*If contact,  $R_2 \gg R_1$ ,*

$$F = \pi d_p \sigma$$

\* *Relative humidity vs. liquid bridge*

$$\ln \left( \frac{p_c}{p_\infty} \right) = \sigma v_m \frac{R_1^{-1} + R_2^{-1}}{kT}$$

*Kelvin equation*



Classification of liquid bridges between particles



(3) *Electrostatic repulsion in liquid media*

Surface charge density

*Surface charging mechanisms in liquid*

- *Preferential adsorption of ions*
- *Dissociation of surface charged species*
- *Isomorphic substitution of ions*
- *Accumulation or depletion of electrons at the surface*
- *Physical adsorption of charged species on to the surface*

*Surface charge varies pH of the medium:*

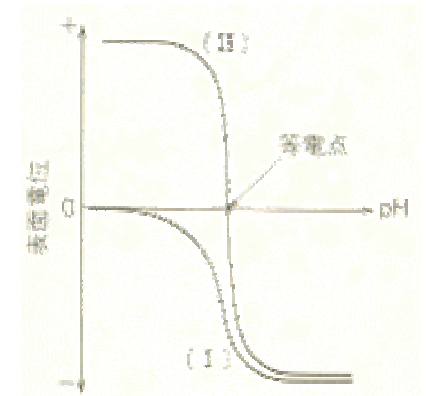
- *Point of zero charge (pzc)*

*For oxides, pH < pzc: positively charged and vice versa*  $pH = -\log[H^+]$

$$E_0 = \frac{2.303RT(pzc - pH)}{F}$$

*At room temperature*

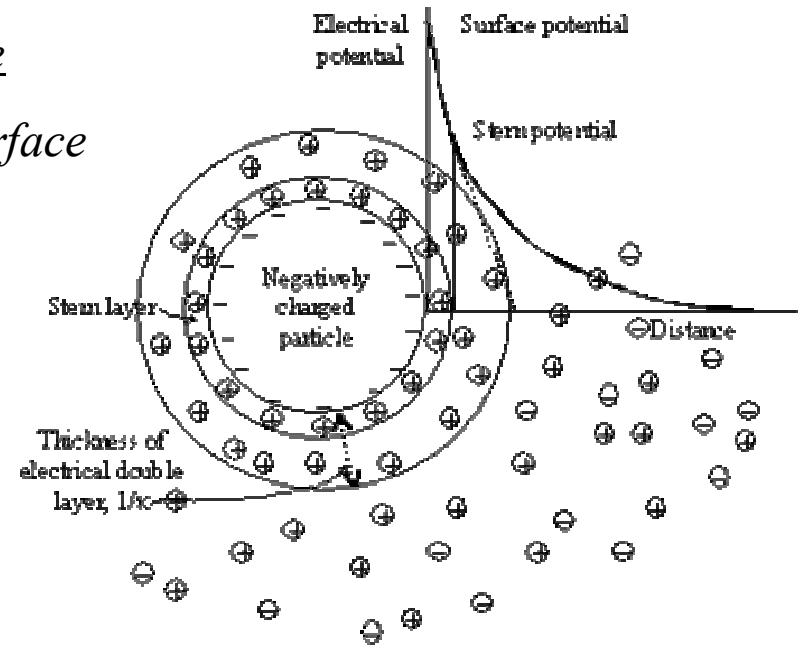
$$E_0 \sim 0.06(pzc - pH)$$



Solids	p.z.c.
WO <sub>3</sub>	0.5
V <sub>2</sub> O <sub>5</sub>	1-2
δ-MnO <sub>2</sub>	1.5
β-MnO <sub>2</sub>	7.3
SiO <sub>2</sub>	2.5
SiO <sub>2</sub> (quartz)	3.7
TiO <sub>2</sub>	6
TiO <sub>2</sub> (calcined)	3.2
SnO <sub>2</sub>	4.5
Al-O-Si	6
ZrO <sub>2</sub>	6.7
FeOOH	6.7
Fe <sub>2</sub> O <sub>3</sub>	8.6
ZnO	8
Cr <sub>2</sub> O <sub>3</sub>	8.4
Al <sub>2</sub> O <sub>3</sub>	9
MgO	12

Electric potential at the proximity of particle surface

- Distribution of electric potential around solid surface
  - Coulombic force or electrostatic force
  - Entropic force, dispersion
  - Brownian motion
- Electrical double layer



Around a charged particle:

- Stern layer : layer of adsorbed counter ions
- Diffuse layer: layer of ions in a balance between electrostatics and diffusion caused by thermal motion.

\* Electrical potential

$$E \propto e^{-\kappa(h-H)}$$

where

$$\kappa = \sqrt{\frac{F^2 \sum_i c_i z_i^2}{\epsilon_r \epsilon_0 RT}}$$

Where  $\kappa$  : inverse of the thickness of electrical double layer

$h$  : distance from the surface

$H$  : Stern layer thickness

$F$  : Faraday constant

$c_i$  : bulk ion concentration

$z_i$  : ionic valence

$\epsilon_0$  : permittivity of vacuum

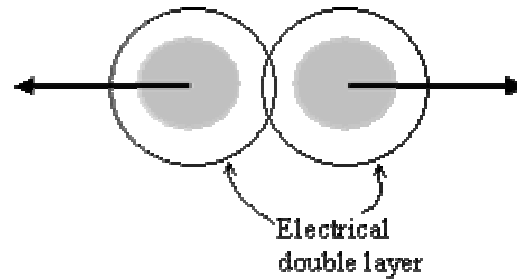
$\epsilon$  : dielectric constant of the solvent

*In water,*

$$\kappa = 3.29 \times 10^9 z_i \sqrt{c_i}$$

*where  $c_i$ : mol/cm<sup>3</sup>*

*Electrical repulsion between two equally sized spherical particles*



$$\Phi_R = \pi \epsilon_r \epsilon_0 d_p E_0^2 e^{-\kappa S}$$

*where  $S$ : the nearest distance from surface to surface*

(4) DLVO Theory (Deryagin - Landau and Vewey Overbeek) theory - In liquid media

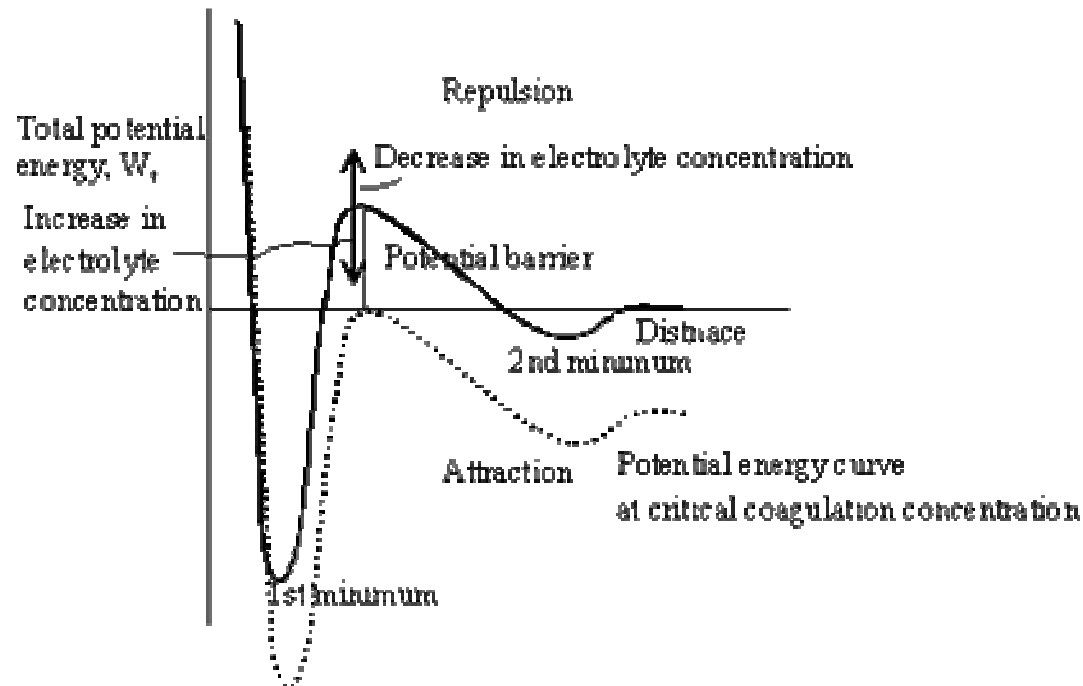
\* Assumptions

*Dilute dispersion (no interference)*

*No other forces besides van der Waals force and electrostatic potential*

*Uniform surface property*       $\Phi = \Phi_A + \Phi_R$

\* Total potential between two particles



- *To increase dispersion of particles*

- *Increase the surface charge or zeta potential .*

*e.g. by adsorption of citrate and chloride ions for gold and*

*hexametaphosphate ion for sulfide semiconductor nanoparticles*

- *Decrease the ionic strength of the dispersing medium.*

- *To coagulate particles*

- *Reduce the surface charge by the displacement of the adsorbed anions by a more strongly bound neutral molecule or cation*

*e.g. adding pyridine to gold sol.*

- *Add electrolytes to the media*

*\*Critical coagulation concentration (CCC)*

- *From  $\Phi = 0$  and  $\frac{d\Phi}{dS} = 0$*

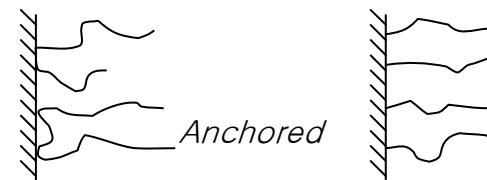
- *Solving two equations simultaneously for  $c_i$*

$$ccc = \frac{107(\epsilon_0 \epsilon_r)^3 k^5 T^6 \sigma^4}{A^2 (Z_i e)^6}$$

(5) Steric stabilization in liquid media

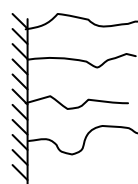
\* *Physically adsorbed vs. anchored (chemically adsorbed)*

*Physically adsorbed*



*Anchored*

\* *Morphologies of polymers adsorbed on particle surface*



*In good solvent*

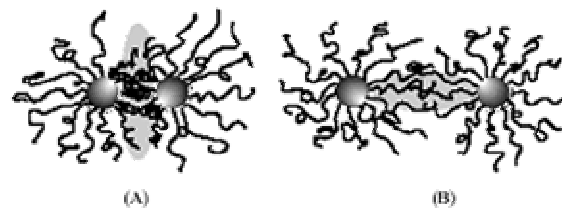


*In poor solvent*

- *The goodness is determined by the nature of polymer-solvent interaction and temperature*

- *Prevention of agglomeration by polymer molecules adsorbed physically or chemically\* on particle surface*

*Entropic effect*       $\Delta G = \Delta H - T\Delta S > 0$



*Osmotic effect: exclusion of solvent between two approaching particles*

*\*Electrostatic vs. steric stabilization*

<i>Electrostatic stabilization</i>	<i>Steric stabilization</i>
<i>Kinetic stabilization</i>	<i>Thermodynamic stabilization</i>
<i>Applicable to dilute particle systems</i>	<i>Applicable to high concentration possible</i>
<i>Sensitive to electrolyte</i>	<i>Insensitive to electrolyte</i>
<i>Unsuitable to multiple phase system</i>	<i>Suitable to multiple phase system</i>

*-Polymers adsorbed also serve as a diffusion barrier to suppress polydisperse growth of particles.*

### ***6.3 Surface modification of nanoparticles***

- *to promote the stability of the particles in liquid media*
- *to alter hydrophilicity of particle surface to hydrophobicity*
- *to couple biomaterials for biological purpose (recognition, delivery, manipulation)*
- *to produce building blocks for assembly (devices)*
- *to obtain functional nanoparticles (core-shell structure)<sup>1</sup>*

#### ***\* Types of surface modification***

- *Anquored /Adsorbed: in-situ/ post-treatment*
- *Core-shell: coating via heterogeneous nucleation route*



*(1) Surface modifiers*

*- Surfactants*

*- Coupling agent (silane)*

*- Polymers*

*\* Choice of surface modifier*

*- Depending on where to be used*

*In general,*

*- requires balance between adsorption vs. affinity to the solvent (good solvent)*

*\* Natural polymer stabilizers: gelatin, agar, cellulose acetate, cellulose nitrate, cyclodextrins*

*- Synthetic polymer stabilizers:*

*- vinyl polymers with polar side groups*

*e.g. polyvinylpyrrolidone, polyvinyl alcohol*

*- vinyl pyrrolidone - vinyl alcohol copolymer (Ag)*

- *Combined effect of electrostatic and steric stabilizations:*
  - *Charged particles with nonionic polymers*
  - *Poly electrolytes attached to uncharged particles*
    - long-chain alkylammonium cations and surfactants*
- *Recent trend*
  - *Use of relatively small ligand*
    - Sulfonated triphenylphosphine, alkanethiol\**

\* *Silane: compounds containing silicon-hydrogen bonds,  $\text{SiH}_4$*

*Trichlorosilane:  $\text{HSiCl}_3$*

*disilane:  $\text{H}_3\text{SiSiH}_3$*

*methylsilane:  $\text{CH}_3\text{SiH}_3$*

*methyldichlorosilane:  $\text{CH}_3\text{SiHCl}_2$*

*triethylsilane:  $(\text{C}_2\text{H}_5)_3\text{SiH}$*

\* *Thiol: sulfur analogous of alcohol*

*"mercaptan"*

*2-mercaptoethanol:  $\text{HSCH}_2\text{CH}_2\text{OH}$*

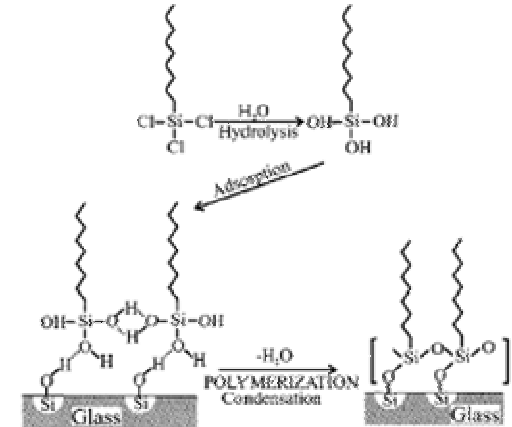
*Mercaptoacetic acid:  $\text{HSCH}_2\text{COOH}$*

*1-amino-2-propanethiol:  $\text{H}_2\text{NCH}_2\text{CH}(\text{SH})\text{CH}_3$*

*Thiophenol:  $\text{C}_6\text{H}_5\text{SH}$*

- *Dithiol:*

*1,2-ethanedithiol:  $\text{HSCH}_2\text{CH}_2\text{SH}$*



Hydrolysis with their  
molecules and surface

(2) Methods of surface modification

- *In situ*

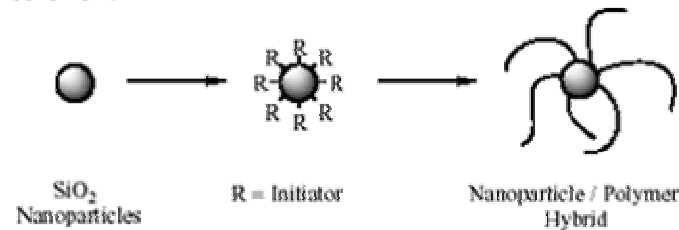
*Preparation from precursor + polymer solution*

*Simultaneous preparation for NP and polymer*

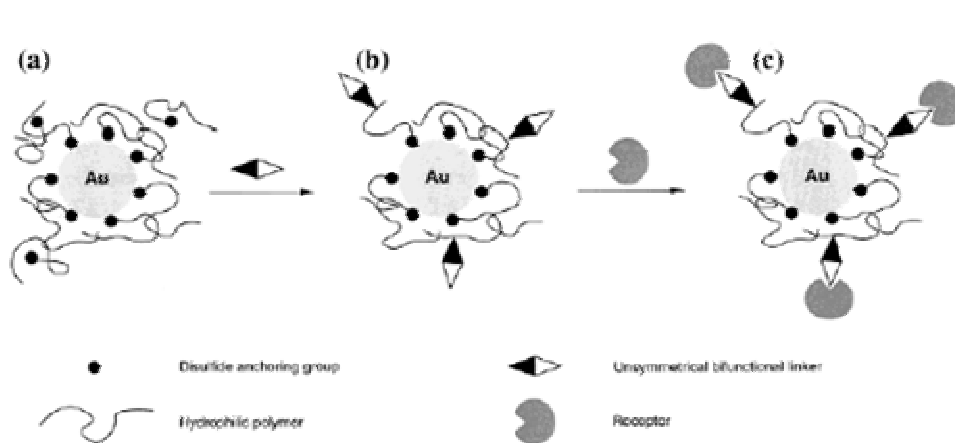
*Preparation from single precursor*

- *Post-treatment*

*Grafting by polymerization from surface-immobilized initiators*



*Grafting to:*



*Stepwise "grafting-to" derivatization of gold surfaces. (a) Fixation of the **polymer with disulfide anchoring groups**. (b) Activation of the polymer*

*Stepwise "grafting-to" derivatization of gold surfaces. (a) Fixation of the **polymer with disulfide anchoring groups**. (b) Activation of the polymer*

*by **unsymmetrical bifunctional linker groups**. (c) Functionalization of the polymer by **receptors**. Step b is omitted when "activated" polymers are used.*

## 6.4 Application of Dispersed Nanoparticles

### (1) Catalysts

#### \* Advantage of nanoparticle catalysts

- very large surface area: "atom economy"

- enhanced **intrinsic chemical reactivity**

*edge and corner effect*

*anion / cation vacancies*

*distorted in bonding patterns*

#### \* Catalyst materials

Metals : Pt (or Pd), Au based, other metals (Cu, V, Rh)

Nonmetallic : MgO, MoS<sub>2</sub>, CeO<sub>2-x</sub>, NiO, Cr<sub>2</sub>O<sub>3</sub>, Fe<sub>2</sub>O<sub>3</sub>, Fe<sub>3</sub>O<sub>4</sub>, Co<sub>3</sub>O<sub>4</sub>, and β-Bi<sub>2</sub>Mo<sub>2</sub>O<sub>9</sub>

#### \* Forms of **dispersed** nanoparticle catalysts

- Homogeneous catalysts: acids, bases, capped nanoparticles

- Heterogeneous catalysts

- dispersed on **highly porous support**(400m<sup>2</sup>/g-600m<sup>2</sup>/g)

*Porous silica, titania, alumina, zeolites*

(2) *Biomedical applications*

*Characteristics of biomaterials:*

- *specific and strong complementary interactions*

*antibody-antigen*

*nucleic acid-DNA*

*hormone-receptor*

*Preparation of biomaterial - nanoparticle conjugates*

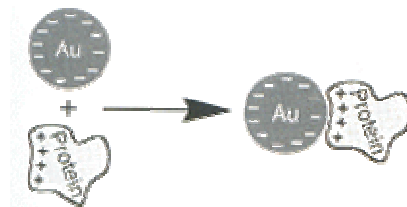
- *Nanoparticles*

- *latex/ gold/ semiconductor/ magnetic nanoparticles*

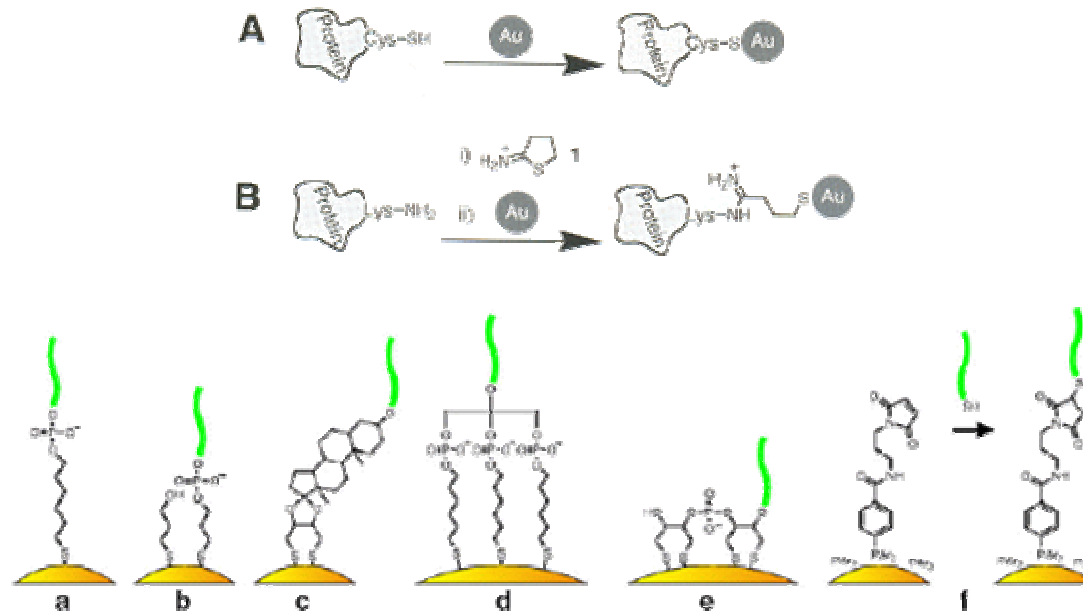
- *Preparation*

- *electrostatic adsorption*

*Au-citrate(-) + protein(+)*



- chemisorption of *thiol-derivatized biomaterials*



Methods for conjugating *oligonucleotides* to *gold nanoparticles*. (a) *Thiol-modified* and (b) *disulfide-modified* oligonucleotides spontaneously bind to gold nanoparticle surfaces. Asymmetric disulfide modification adds an additional *mercaptoalcohol ligand* to the Au surface, but the density of oligonucleotides formed on the nanoparticle surface is the same as for thiol-terminal oligonucleotides. (c) *Di* and (d) *tri-sulfide modified* conjugates. (e) *Oligothiols-nanoparticle* conjugates. Although four thiol connections are shown, any number are possible via sequential addition of a commercial dithiane phosphoramidite during solid-phase oligonucleotide synthesis. (f) Oligonucleotide conjugates from *Nanoprobes' phosphine-modified* nanoparticles

## Applications

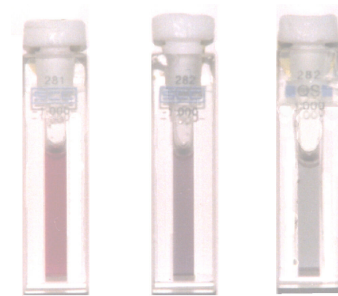
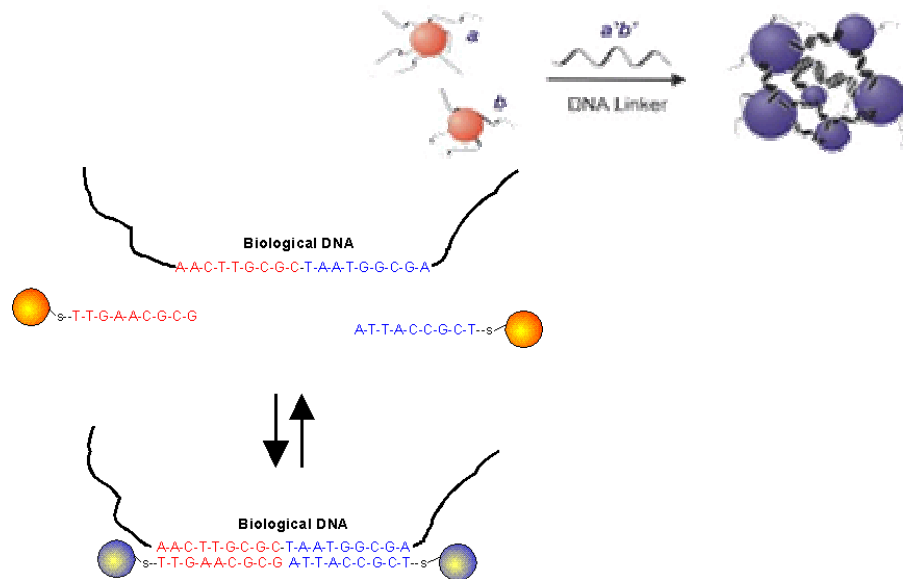
For Nanoparticle-DNA, see

[http://www.ipht-jena.de/BEREICH\\_3/english/molnano/pdf/36.pdf](http://www.ipht-jena.de/BEREICH_3/english/molnano/pdf/36.pdf)

For Biomaterial-functionalized magnetic nanoparticles, see

<http://www.biomagres.com/content/1/1/2>

### - **Reporter** for biochemical information (labeling, sensor)

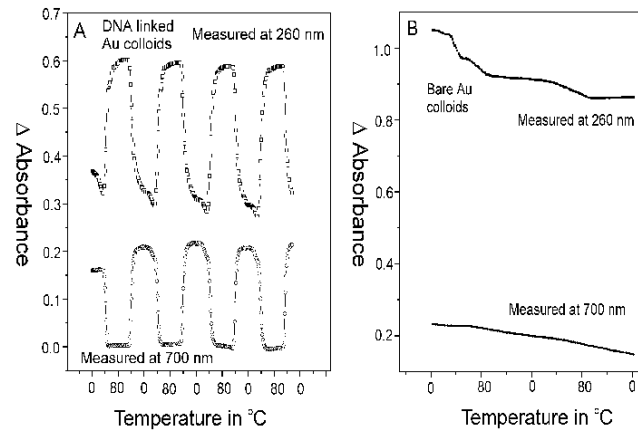


*Cuvettes containing the DNA modified Au colloids and linking strands.*

*This scheme illustrates how a targeted portion of biological DNA can be used as the linker molecule to aggregate DNA modified colloids. Applications of this described system include **sequence specific gene detection and DNA separation methodologies.***

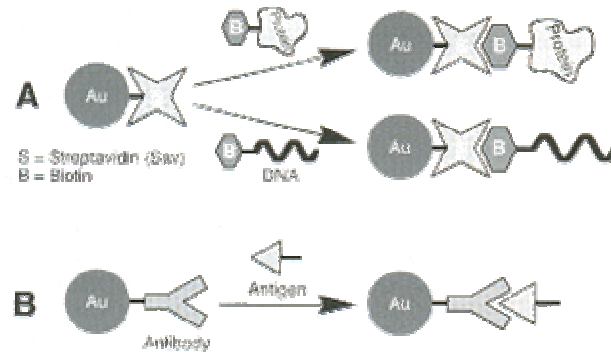


- *Reversible hybridization*



A) Absorbance vs. temperature/time profile for DNA/colloid hybridized materials. At low temperatures the Au colloids aggregate due to the hybridization of "linking" DNA. At high temperatures (80 degrees Centigrade), the colloids are dehybridized and form a dark red solution. The temperature vs. time profile shows that this is a reversible process. B) Same analysis of an aqueous solution of **unmodified Au colloids**.

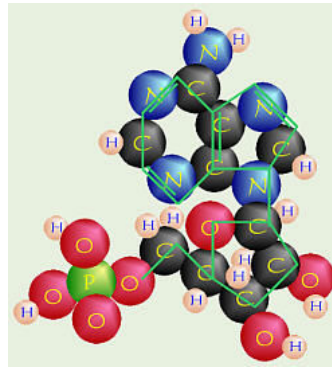
- *Capturer for bioseparation of molecules or cells*



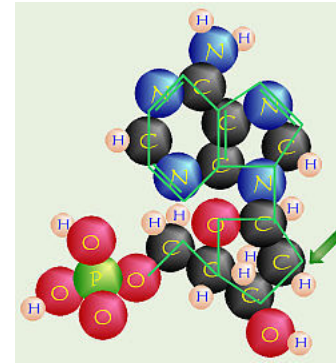
- *Drug carrier*
- *Gene carriers*

\* **DNA (deoxyribonucleic acid)** [http://library.thinkquest.org/18617/index-java\\_frames.html](http://library.thinkquest.org/18617/index-java_frames.html)

- **Nucleotide molecules**

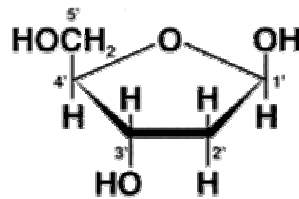


Nucleotide

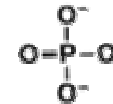


Deoxynucleotide

**Deoxyribose sugar**



**Phosphate group**



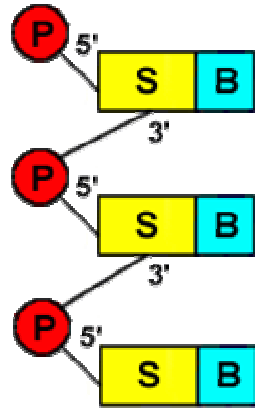
**Nucleotide bases**

Base	Adenine (A)	Guanine (G)	Thymine (T)	Cytosine (C)
Purine/ Pyrimidine	Purine	Purine	Pyrimidine	Pyrimidine
Chemical Structure *				
Simplified Representation				

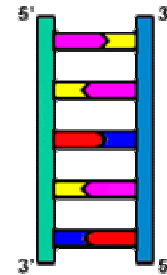
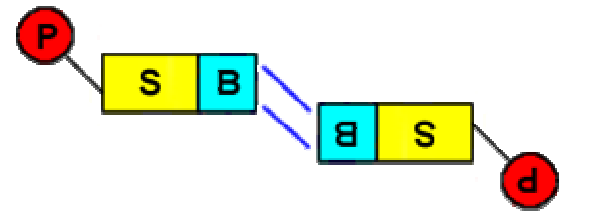
\* C = Carbon, N = Nitrogen, O = Oxygen.  
A single line between atoms is a single bond.  
A double line between atoms is a double bond.

- Structures

*Helix*



*Base pairing*



- Adenine
- Thymine
- Guanine
- Cytosine

*Compacted double stranded (helix) nucleotides nanowires*

