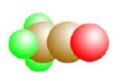
### Applied Statistical Mechanics Lecture Note - 7





## **Optimization Techniques**

고려대학교 화공생명공학과 강정원

## Introduction





- Optimization
  - ☐ Finding stationary point of a function
- Methods
  - Steepest Descent
  - Conjugate Gradient Method
  - Newton-Raphson Method
  - Locating the Global Minimum and Conformal Sampling
    - Stochastic and Monte Carlo Method
    - Molecular Dynamics
    - Simulated Annealing
    - Genetic Algorithm
    - Diffusion Method
    - Distance Geometry Method

### Local Minimum vs. Global Minimum





- Steepest Descent
- Conjugate Gradient Method
- Newton' Method
  - → Local Minimum Methods ("Nearest minimum")
- A global optimization is an extremely difficult task for a multidimensional problem
  - Multiple minima
  - Combinatorial expolsion

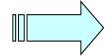
### Possible conformation for linear alkanes





$$CH_3 (CH_2)_{n+1} (CH_3)$$

N	No. of possible conformation 3 <sup>n</sup>	Time 1 conformation = 1 s
1	3	3s
5	243	4 min
10	59049	16 h
15	14348907	166 d



**Combinatorial explosion!** 

The systematic (or grid) search is only possible for small molecules

### Stochastic and Monte Carlo Method





- Similar to MC simulation of properties
- Procedure
  - Random "kick" is generated to one or more atoms
  - New geometry is accepted if the lower energy
  - □ Otherwise Boltzmann factor is calculated and compared with random number between (0,1)

# Molecular Dynamics





- Solves Newton's second law of motion for atoms on an energy surface
- $\blacksquare$  Available energy = (kinetic) + (potential)
  - ☐ Molecules are able to overcome barriers separating munima if sufficient kinetic energy is given
  - □ Closely related to the temperature of the system
  - ☐ Require long simulation time

# Simulated Annealing





- MC and MD employ a temperature as guiding parameter
- At sufficiently high T and long time, conformation space is sampled
- Simulated Annealing (SA)
  - ☐ Initial T is chosen to be high (2000-3000K)
  - ☐ MC and MD run
  - ☐ T is slowly reduced (Trapped in minimum)

# Genetic Algorithm





- Concept and terminology from biology
- Children = mixture of parent genes
  - ☐ Allowing mutation of parent genes
  - ☐ Best population are seelected based on Darwin's principle