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2004 춘계화학공학회

# Density measurement with the vibrating tube densimeter

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# Objectives

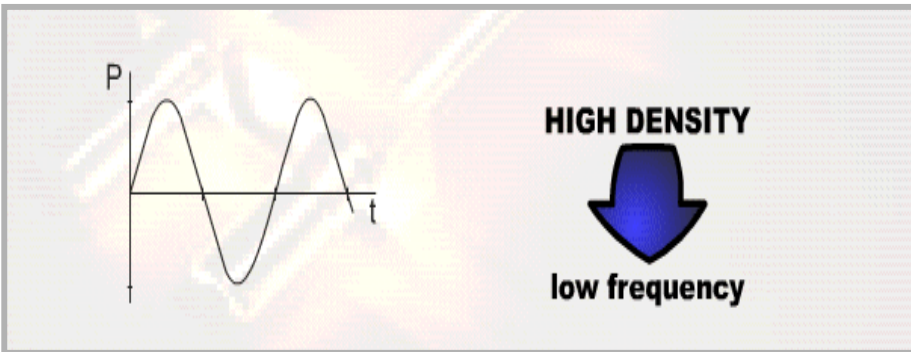
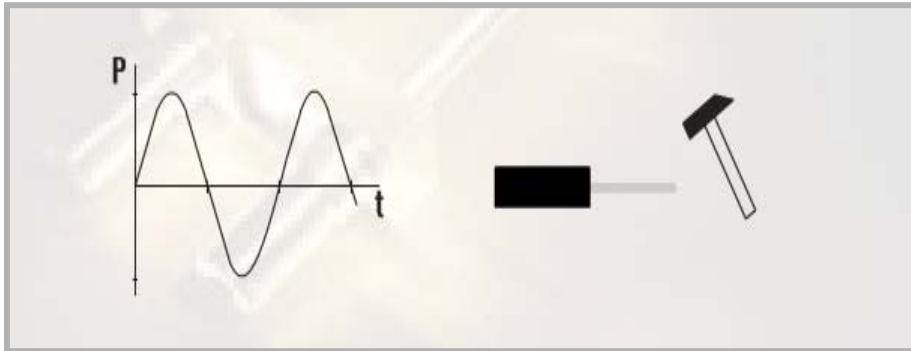
- 초임계를 포함한 고온, 고압영역까지 Density를 측정할 수 있는 실험 장치를 설계 및 고안.
- 기준물질로 water와 vacuum을 이용하여 Densimeter 보정.
- CO<sub>2</sub> period를 측정하여 Densimeter 보정식으로 결정된 Density를 보고 된 실험결과와 비교, 검토하여 실험장치의 건전성 확인.



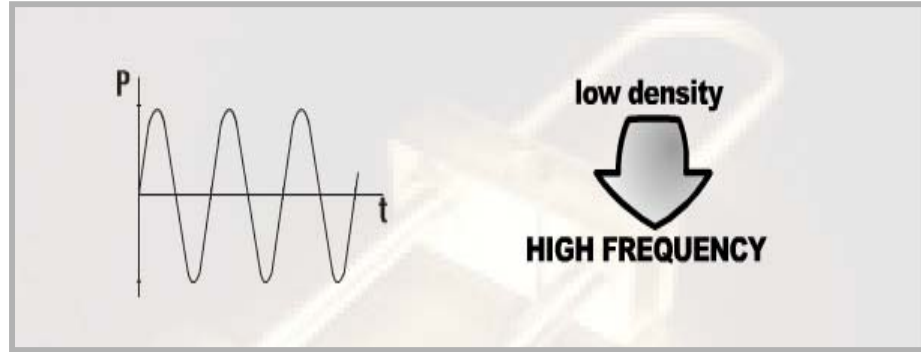
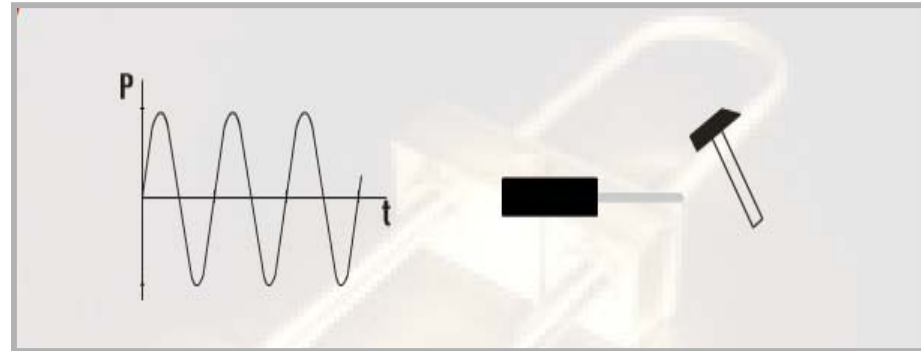
# Introduction

## • U-tube method principle

### ◆ U- tube filled with water



### ◆ U- tube filled with vacuum



# Introduction

- Anton Paar DMA 512P



<b>Cell material:</b>	Hastelloy C-276
<b>Temperature range:</b>	-10 to +150 °C (14 to 302 °F)
<b>Pressure range:</b>	0 to 700 bar (0 to 10,000 psi)
<b>Density range:</b>	0 to 3 g/cm <sup>3</sup>
<b>Density resolution:</b>	1 x 10E-5g/cm <sup>3</sup>
<b>Density repeatability:</b>	±1 x 10E-5 g/cm <sup>3</sup>
<b>Accuracy:</b>	1 x 10E-3 g/cm <sup>3</sup> up to 3 x 10E-5 g/cm <sup>3</sup>
<b>Volume of the measuring cell:</b>	Approx. 2,5 cm <sup>3</sup>
<b>Temperature coefficient of the measuring cell:</b>	Typically -3 x 10E-3 g/cm <sup>3</sup> /K
<b>Pressure coefficient of the measuring cell:</b>	Typically 2 x 10E-5 g/cm <sup>3</sup> /bar
<b>Dimensions / Weight:</b>	320 x 120 x 430 / 25 kg
<b>Power supply:</b>	110/220 V a.c., 60/50 Hz
<b>Connections:</b>	Pressure fittings for metal tubes with 1/8" outer diameter



# Introduction

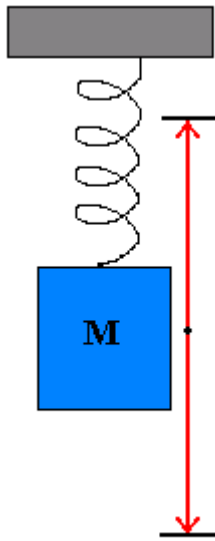
## • Comparison

	Hydrometer	Pycnometer	U-Tube
Volume of sample	> 100 ml	10 to 100 ml	1 ml
Time per measurement	A few minutes	A few hours	A few minutes
Uncertainty of measurement	$10^{-3}$ to $10^{-4}$ g/cm <sup>3</sup>	$10^{-4}$ to $10^{-5}$ g/cm <sup>3</sup>	$10^{-3}$ to $10^{-5}$ g/cm <sup>3</sup>
Repeatability	$10^{-3}$ to $10^{-4}$ g/cm <sup>3</sup>	$10^{-3}$ to $10^{-4}$ g/cm <sup>3</sup>	$10^{-4}$ to $10^{-6}$ g/cm <sup>3</sup>
Limiting factors	Temperature Surface tension Human influence	Temperature Volume determination Human influence	Dynamic effects



# Results

- Calibration method



$$f = \frac{1}{2\pi} \sqrt{\frac{C}{M}} = \frac{1}{2\pi} \sqrt{\frac{C}{M_u + \rho V_u}}$$

$$\tau = 2\pi \sqrt{\frac{M_u + \rho V_u}{C}}$$

$M_u$  ; The mass of tube

$V_u$  ; The internal volume of tube

$C$  ; Elasticity constant

$$\rho(T, P) = A(T, P) \times \tau^2(T, P) - B(T, P)$$



# Introduction

- Case I ) At constant T and P

$$\rho = A \times \tau^2 - B$$

$$A = \frac{\rho_1 - \rho_2}{P_1^2 - P_2^2}$$

$$B = \frac{\tau_2^2 \times \rho_1 - \tau_1^2 \times \rho_2}{\tau_1^2 - \tau_2^2}$$

$\rho$  ; unknown density of sample

$\rho_1$  ; density of reference 1

$\rho_2$  ; density of reference 2

$\tau_1$  ; Period of reference 1

$\tau_2$  ; Period of reference 2

$\tau$  ; Period of sample



# Introduction

- Case II ) Over wide T and P ranges

$$\rho(T, P) = \rho_w(T, P) + \frac{\rho_w(T, 1)}{\tau_w^2(T, 1) - \tau_v^2(T)} [\tau^2(T, P) - \tau_w^2(T, P)]$$

$\rho$  ; unknown density of sample

$\rho_w$

$\tau_v$  ; the period of vacuum

$\tau$  ; the period of sample

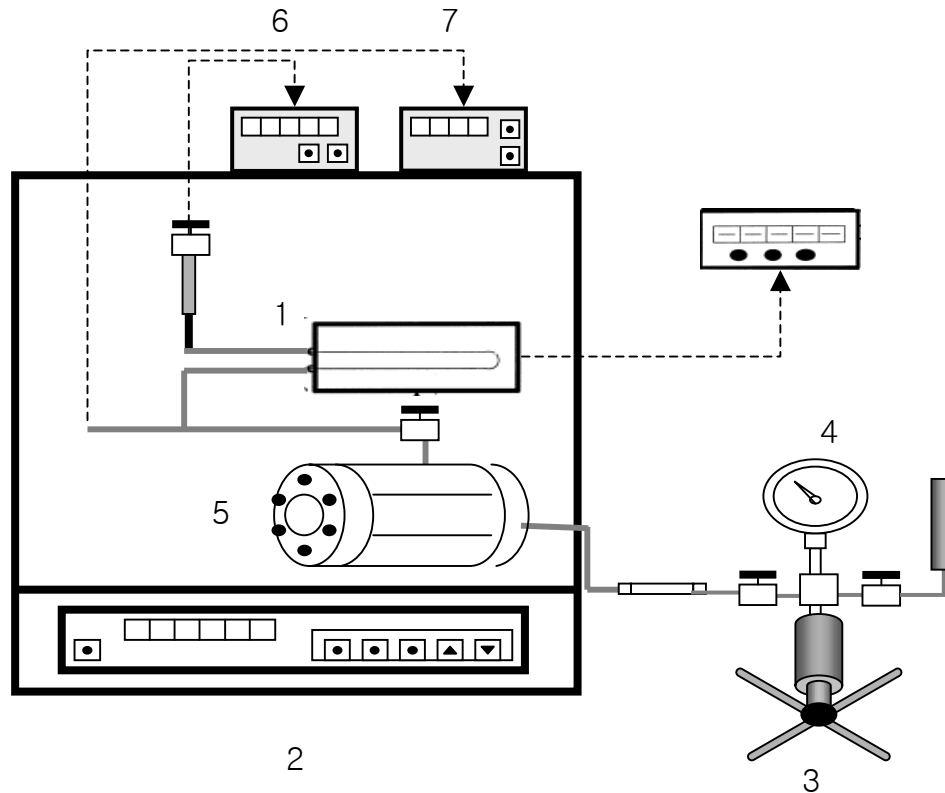
$\tau_w$  ; the period of water





# Experimental Apparatus

- water

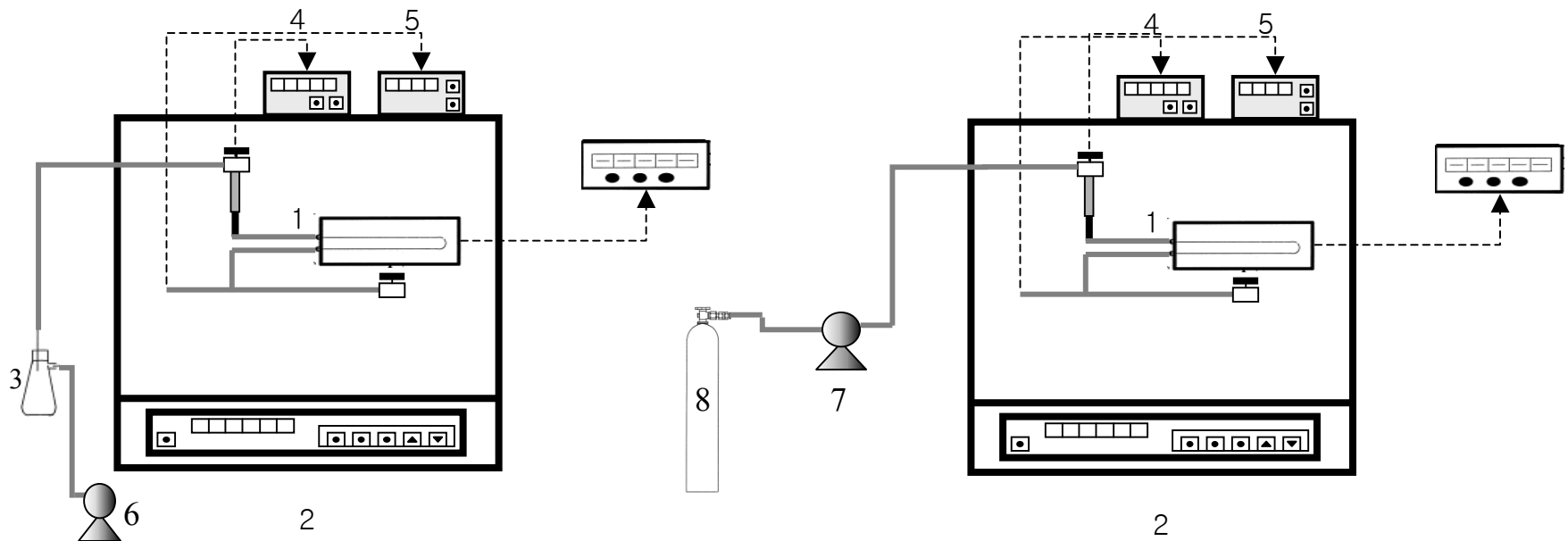


1. U-tube
2. Air bath
3. Hand pump
4. Pressure gauge
5. View cell
6. Digital pressure transducer
7. RTD Indicator



# Experimental Apparatus

- vacuum , CO<sub>2</sub>



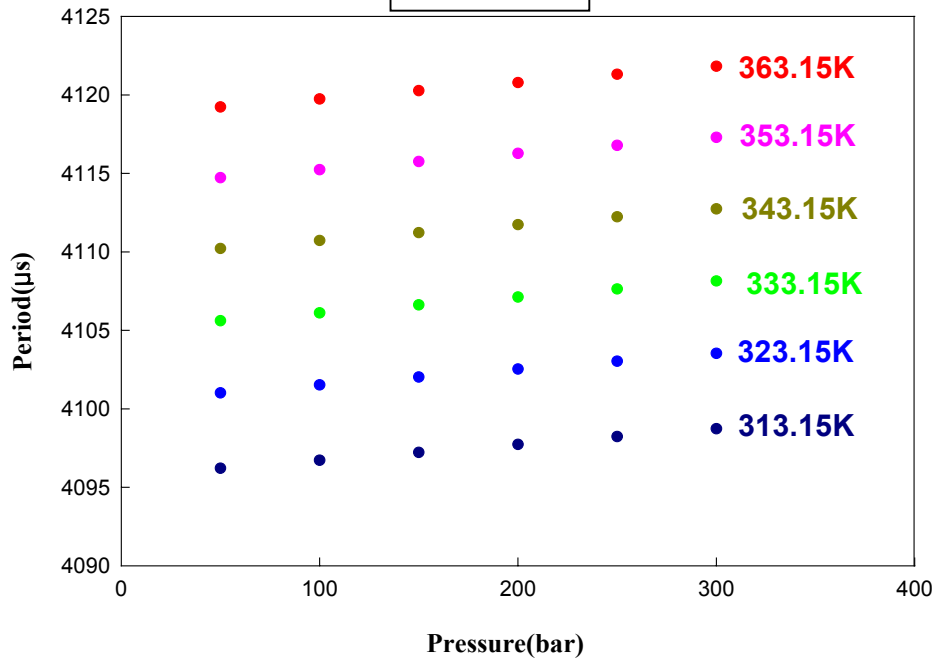
- |    |          |    |                             |    |                       |
|----|----------|----|-----------------------------|----|-----------------------|
| 1. | U-tube   | 4. | Digital pressure transducer | 7. | Gas booster           |
| 2. | Air bath | 5. | RTD Indicator               | 8. | CO <sub>2</sub> bombe |
| 3. | Trap     | 6. | Vacuum pump                 |    |                       |



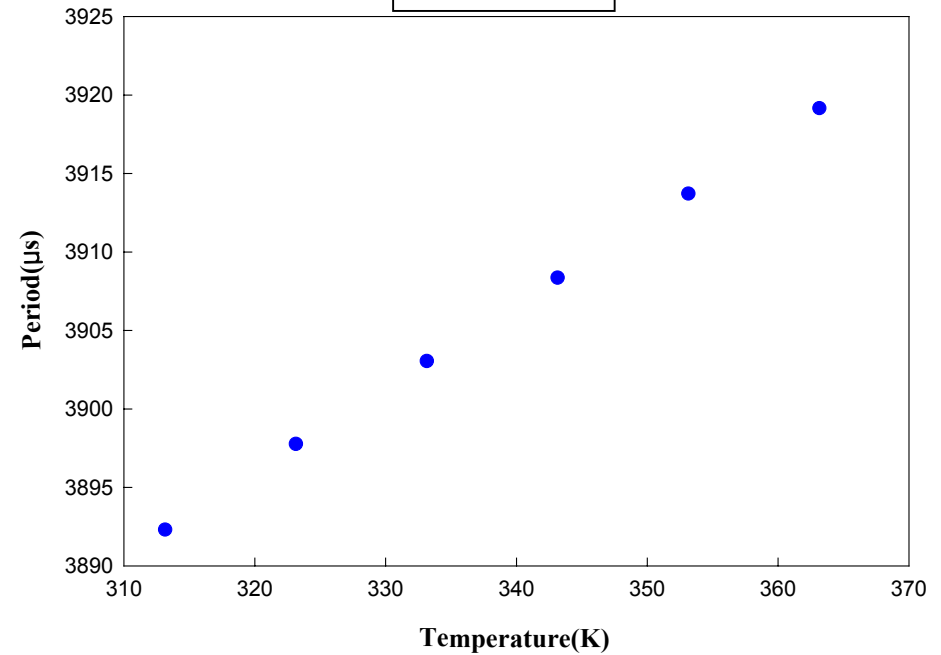
# Results

## • Period of water and vacuum

Period of water

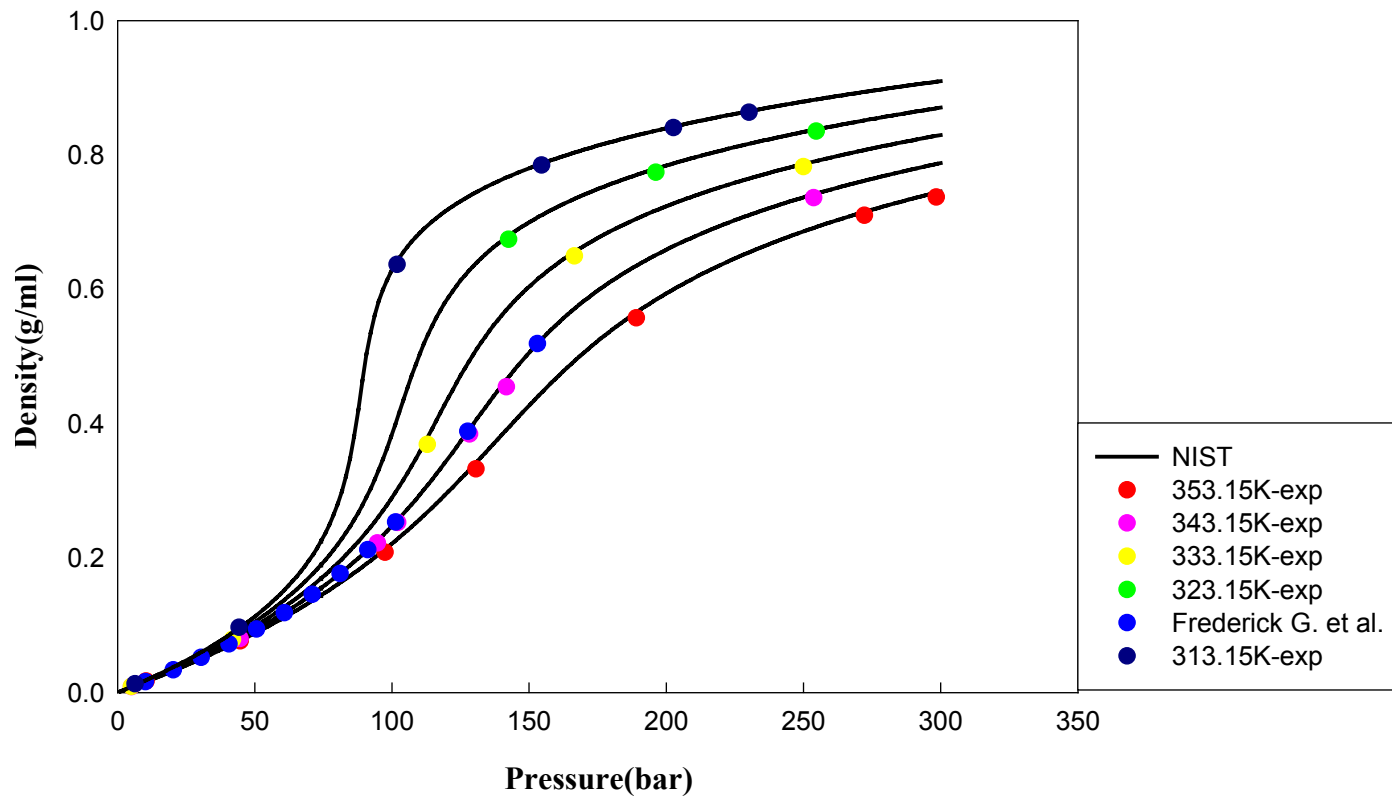


Period of vacuum



# Results

## • Density of CO<sub>2</sub>



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## Conclusions

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- U-tube method를 이용하여 고온, 고압 및 초임계까지 density를 측정할 수 있는 실험장치를 설계 및 고안하였다.
- 기준물질로 water와 vacuum의 period를 측정하여 보정하였다.
- CO<sub>2</sub> period를 측정하여 densimeter 보정식으로 결정된 density를 보고된 실험결과와 비교, 검토하여 실험장치의 건전성을 확인하였다.
- 광범위한 온도, 압력조건에서 순수 물질과 혼합물질의 density를 측정하는데 활용할 수 있다.

